

# Alternatives to SUSY

*SUSY 2011 conference*

*Fermilab, August 28 - Sept. 2 2011*

*Christophe Grojean*

CERN-TH & CEA-Saclay/IPhT

( [christophe.grojean@cern.ch](mailto:christophe.grojean@cern.ch) )



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# The UV behavior of the weak Goldstone

symmetry breaking: new phase with more degrees of freedom

massive  $W^\pm, Z$ : 3 physical polarizations=eaten Goldstone bosons  $\frac{SU(2)_L \times SU(2)_R}{SU(2)_V}$

—————  $\Rightarrow$  UV behavior of these Goldstone's?  $\Leftarrow$  —————

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see e.g. Hosotani's talk yesterday

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*At which scale should we expect to see something?*

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$$\Sigma = e^{i\sigma^a \pi^a / v}$$

Goldstone of  
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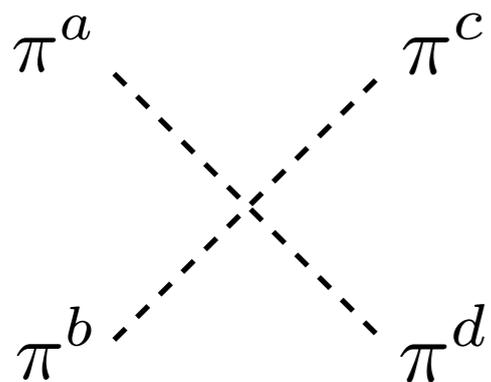
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contact interaction growing with energy

$$\mathcal{A}(\pi^a \pi^b \rightarrow \pi^c \pi^d) = \mathcal{A}(s, t, u) \delta^{ab} \delta^{cd} + \mathcal{A}(t, s, u) \delta^{ac} \delta^{bd} + \mathcal{A}(u, t, s) \delta^{ad} \delta^{bc}$$

$$\mathcal{A}(s, t, u) = \frac{s}{v^2} \quad \text{Weinberg's LET}$$



Lee, Quigg & Thacker '77

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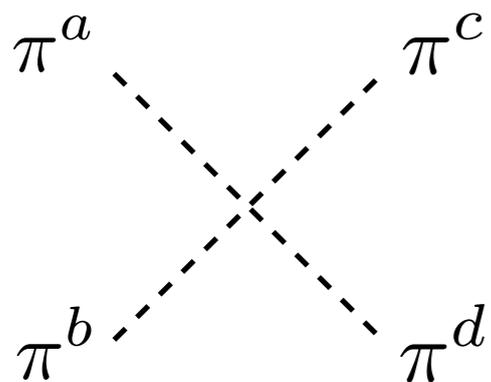
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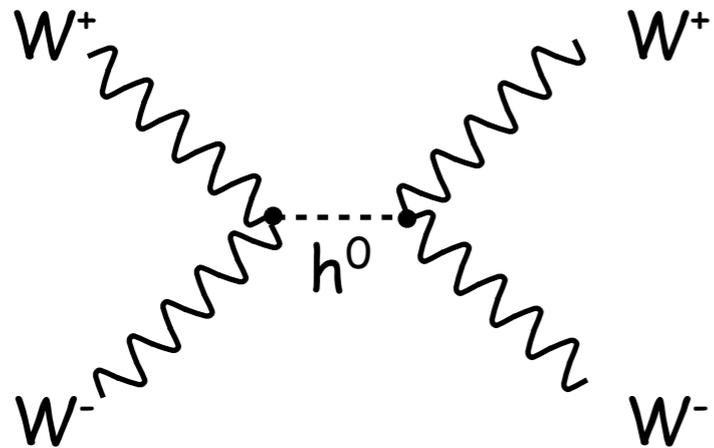
the behavior of this amplitude is not consistent above  $4\pi v$  ( $\approx 1-3 \text{ TeV}$ )

Lee, Quigg & Thacker '77

# Weak vs. Strong EWSB

what is unitarizing the WW scattering amplitude?

Weakly coupled models



prototype: Susy  
susy partners  $\sim 100$  GeV

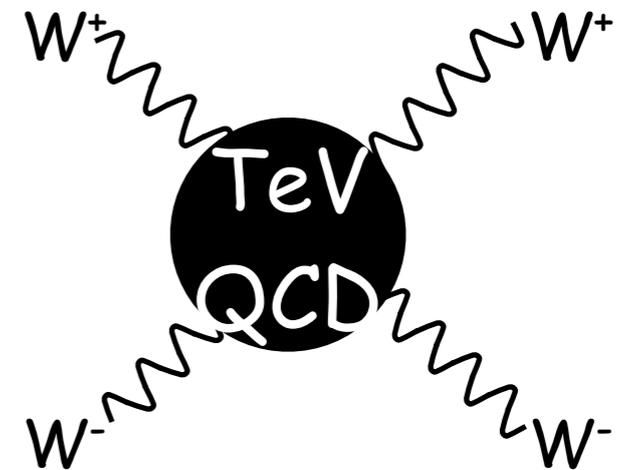
need new particles to stabilize  
the Higgs mass

bounds on the masses of these particles



fine-tuning  $O(1\%)$

Strongly coupled models



prototype: Technicolor  
rho meson  $\sim 1$  TeV

resonances needed for unitarization  
generate EW oblique corrections

$$\hat{S} \sim \frac{m_W^2}{m_\rho^2} \quad \begin{array}{l} |\hat{S}| < 10^{-3} \\ \longrightarrow \\ @95\% \text{ CL} \end{array} \quad m_\rho > 2.5 \text{ TeV}$$

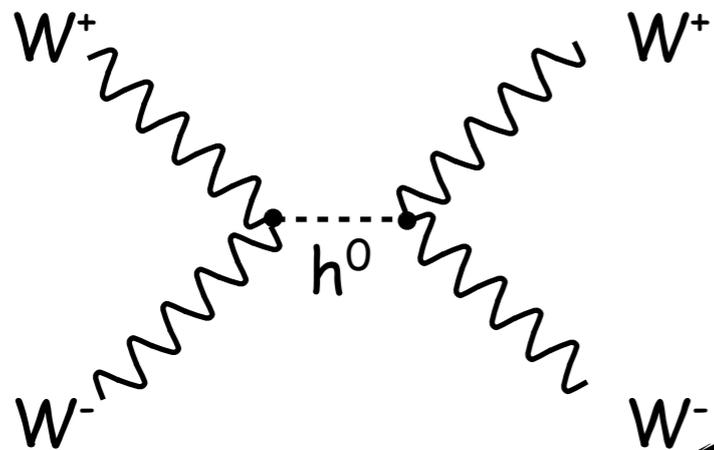
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# Weak vs. Strong EWSB

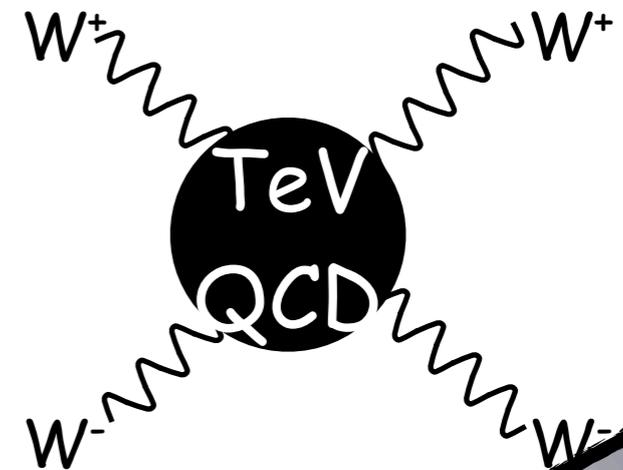
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Weakly coupled models

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other ways?



prototype:

susy part

symmetry

needed new particles to stabilize the Higgs mass

bounds on the masses of these particles



fine-tuning O(1%)

prototype:

dynamics

resonances needed for unitarization generate EW oblique corrections

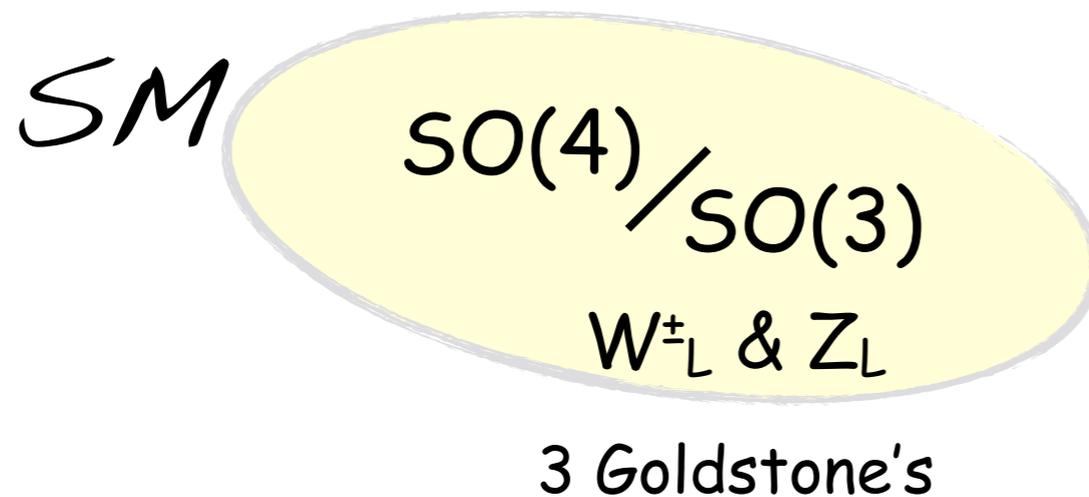
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# Higgs as a PGB: a natural extension of SM

One solution to the hierarchy pb:

Higgs transforms non-linearly under some global symmetry

Higgs=Pseudo-Goldstone boson (PGB)



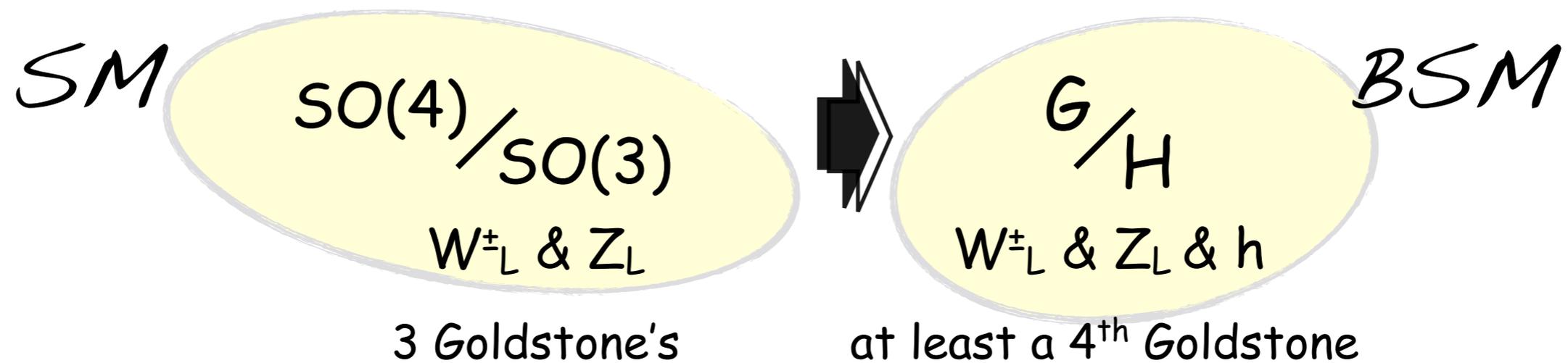
Chacko, Batra '08

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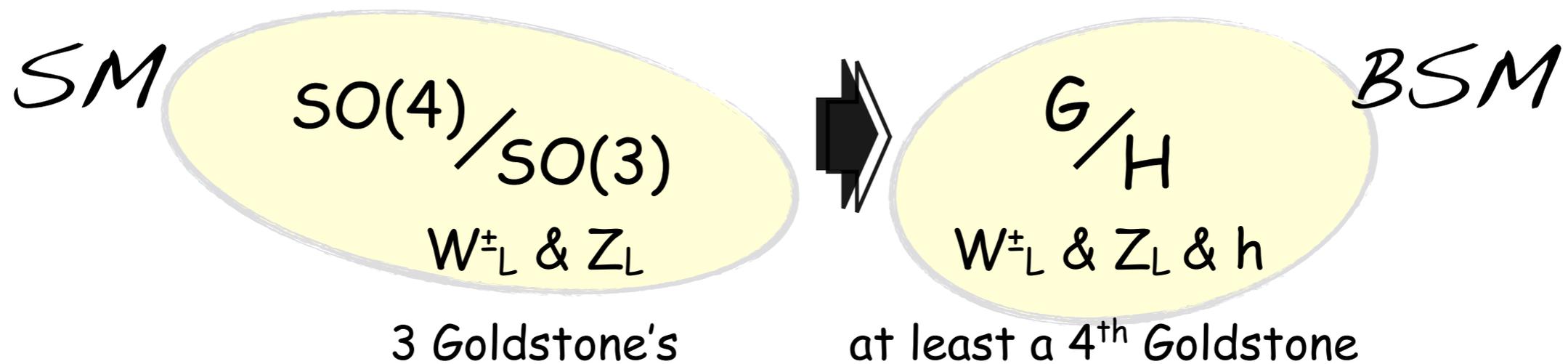
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Examples:  $SO(5)/SO(4)$ : 4 PGBs= $W^\pm_L, Z_L, h$

Minimal Composite Higgs Model

Agashe, Contino, Pomarol '04

$SO(6)/SO(5)$ : 5 PGBs= $H, a$

Next MCHM

Gripaios, Pomarol, Riva, Serra '09

Chacko, Batra '08

$SU(4)/Sp(4, \mathbb{C})$ : 5 PGBs= $H, s$

$SO(6)/SO(4) \times SO(2)$ : 8 PGBs= $H_1 + H_2$

Minimal Composite Two Higgs Doublets

Mrazek, Pomarol, Rattazzi, Serra, Wulzer '11

*How to probe the composite nature of the Higgs?*

*1. Anomalous couplings*

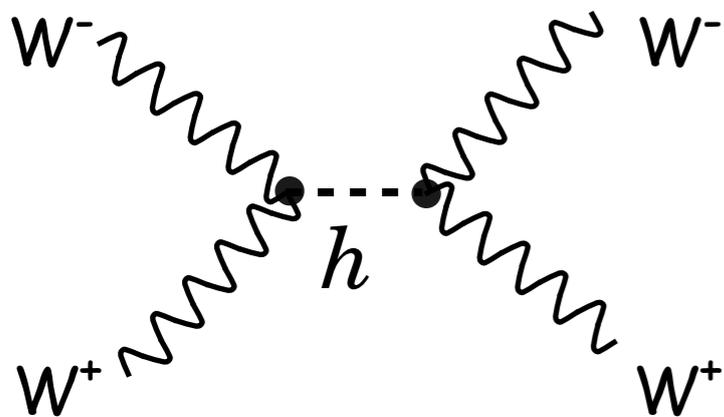


# What is the SM Higgs?

A single scalar degree of freedom neutral under  $SU(2)_L \times SU(2)_R / SU(2)_L$

$$\mathcal{L}_{\text{EWSB}} = \frac{v^2}{4} \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma) \left( 1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} \right) - \lambda \bar{\psi}_L \Sigma \psi_R \left( 1 + c \frac{h}{v} \right)$$

'a', 'b' and 'c' are arbitrary free couplings



$$\mathcal{A} = \frac{1}{v^2} \left( s - \frac{a^2 s^2}{s - m_h^2} \right)$$

growth cancelled for  
 $a = 1$   
 restoration of  
 perturbative unitarity

Cornwall, Levin, Tiktopoulos '73

Contino, Grojean, Moretti, Piccinini, Rattazzi '10

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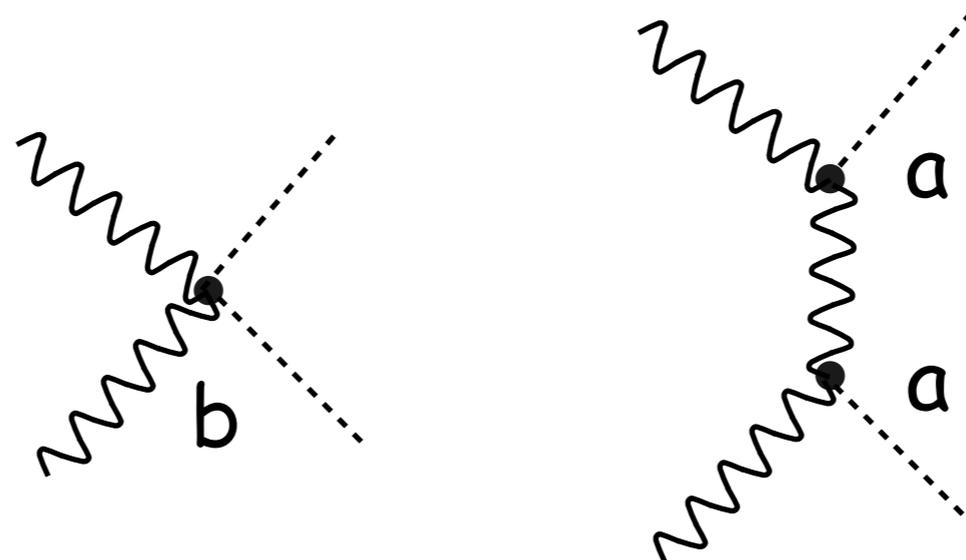
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For  $a=1$ : perturbative unitarity in elastic channels  $WW \rightarrow WW$

For  $b = a^2$ : perturbative unitarity in inelastic channels  $WW \rightarrow hh$

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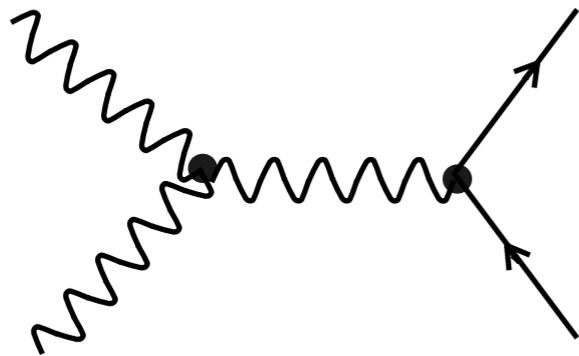
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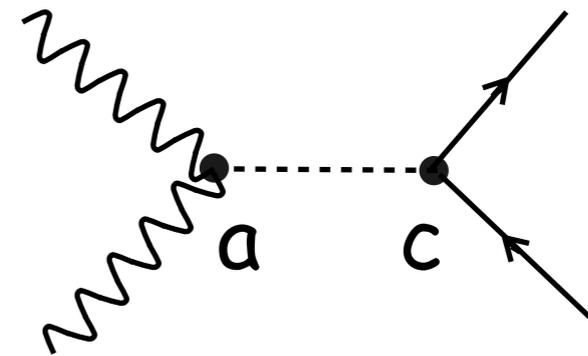
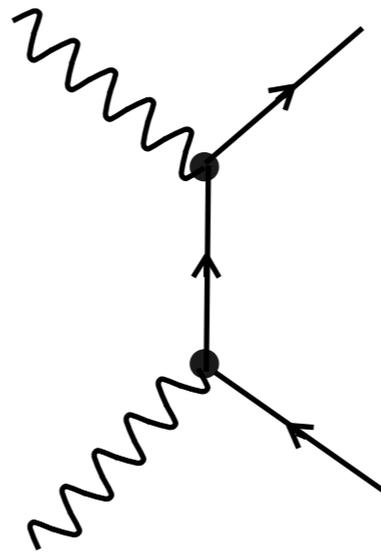
For  $b = a^2$ : perturbative unitarity in inelastic channels  $WW \rightarrow hh$

For  $ac=1$ : perturbative unitarity in inelastic  $WW \rightarrow \psi \psi$

Cornwall, Levin, Tiktopoulos '73



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For  $b = a^2$ : perturbative unitarity in inelastic channels  $WW \rightarrow hh$

For  $ac=1$ : perturbative unitarity in inelastic  $WW \rightarrow \psi \psi$

'a=1', 'b=1' & 'c=1' define the SM Higgs

Higgs properties depend on a single unknown parameter ( $m_H$ )

$\mathcal{L}_{\text{EWSB}}$  can be rewritten as  $D_\mu H^\dagger D_\mu H$

$$H = \frac{1}{\sqrt{2}} e^{i\sigma^a \pi^a / v} \begin{pmatrix} 0 \\ v + h \end{pmatrix}$$

$h$  and  $\pi^a$  (ie  $W_L$  and  $Z_L$ ) combine to form a linear representation of  $SU(2)_L \times U(1)_Y$

# What is a composite Higgs?

A  $\sigma$  particle that combines with  $W_L$  and  $Z_L$  to form a  $SU(2)$  doublet that acquires a vev

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*renormalizable level = uniqueness*

*non-renormalizable level*

$SU(2)_L \times U(1)_Y$  linearly realized &  $a, b, c \neq 1 \Leftrightarrow$  Composite Higgs

deviations of Higgs couplings originate from higher dimensional operators

$$\left(\partial_\mu |H|^2\right)^2 \quad |H|^2 \bar{\psi} H \psi \quad |H|^2 B_{\mu\nu} B^{\mu\nu} \quad |H|^2 G_{\mu\nu} G^{\mu\nu}$$

# Anomalous composite-Higgs couplings

Giudice, Grojean, Pomarol, Rattazzi '07

$$\mathcal{L} \supset \frac{c_H}{2f^2} \partial^\mu (|H|^2) \partial_\mu (|H|^2) \quad c_H \sim \mathcal{O}(1)$$

$$H = \begin{pmatrix} 0 \\ \frac{v+h}{\sqrt{2}} \end{pmatrix} \Rightarrow \mathcal{L} = \frac{1}{2} \left( 1 + c_H \frac{v^2}{f^2} \right) (\partial^\mu h)^2 + \dots$$

Modified  
Higgs propagator

$\sim$

Higgs couplings  
rescaled by

$$\frac{1}{\sqrt{1 + c_H \frac{v^2}{f^2}}} \sim 1 - c_H \frac{v^2}{2f^2} \equiv 1 - \xi/2$$

$$\xi = v^2/f^2$$

$$a = 1 - \xi/2 \quad b = 1 - 2\xi \quad c = 1 - \xi/2$$

# PGB Higgs: Strong EWSB with 2 Scales

$$\xi = \frac{v^2}{f^2} = \frac{(\text{weak scale})^2}{(\text{strong coupling scale})^2}$$

$$\xi = 0$$

SM limit

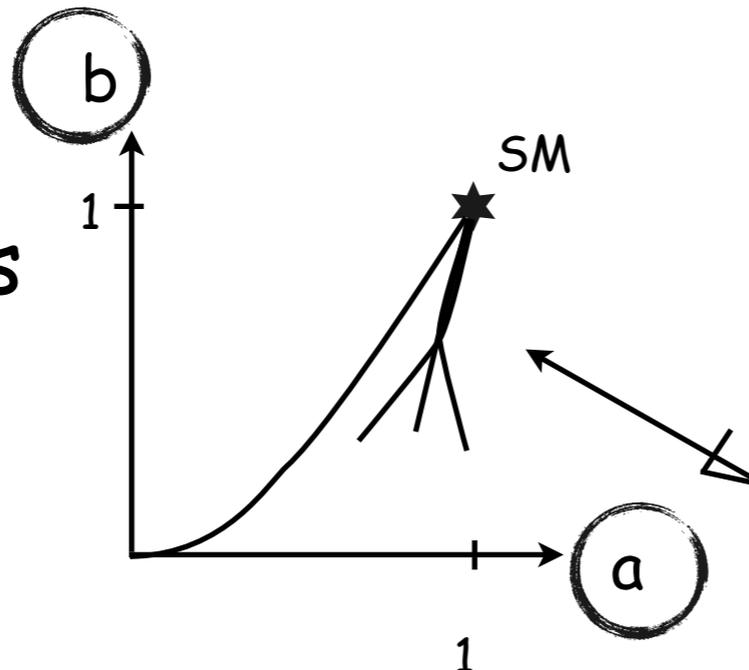
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$$\xi = 1$$

Technicolor limit

Higgs decouple from SM; vector resonances like in TC

Composite Higgs  
vs.  
SM Higgs



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universal behavior for large  $f$   
 $a=1-v^2/2f^2$   $b=1-2v^2/f^2$

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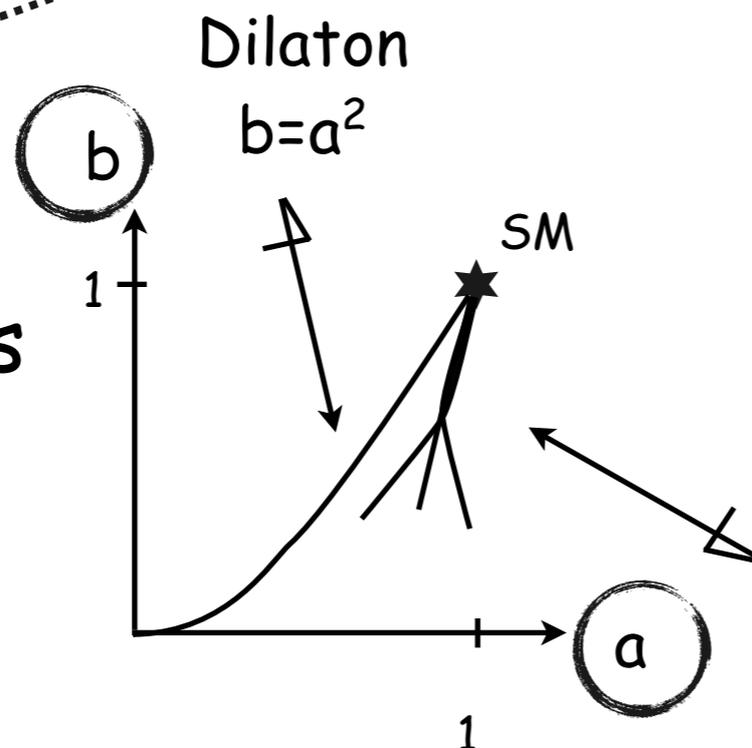
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 $a = 1 - v^2/2f^2$   $b = 1 - 2v^2/f^2$

# Composite Higgs vs generic anomalous couplings

generic anomalous couplings can be quite complicated, e.g.

$$\mathcal{L}_{h-Z} = m_Z h \left( c_1 Z_\mu Z^\mu + \frac{c_2}{m^2} Z_{\mu\nu} Z^{\mu\nu} + \frac{c_3}{m^2} \epsilon_{\mu\nu\rho\sigma} Z^{\mu\nu} Z^{\rho\sigma} \right)$$

...many coefficients, various possible origins

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...many coefficients, various possible origins

if Higgs emerges as a bound state of strongly interacting theory

a few coefficients only and related to symmetries of the coset space

$$\frac{c_H}{2f^2} \left( \partial^\mu |H|^2 \right)^2$$

$$\frac{c_T}{2f^2} \left( H^\dagger \overleftrightarrow{D}^\mu H \right)^2$$

custodial breaking

$$\frac{c_y y_f}{f^2} |H|^2 \bar{f}_L H f_R + \text{h.c.}$$

$$\frac{c_6 \lambda}{f^2} |H|^6$$

(other resonances etc give subleading contributions)

very predictive models:

given the coset space, the Higgs couplings depend only on  $\xi$

# Effective Lagrangian

Giudice, Grojean, Pomarol, Rattazzi '07

■ extra Higgs leg:  $H/f$

■ extra derivative:  $\partial/m_\rho$

■ **Genuine strong operators** (sensitive to the scale  $f$ )

$$\frac{c_H}{2f^2} \left( \partial^\mu |H|^2 \right)^2$$

$$\frac{c_T}{2f^2} \left( H^\dagger \overleftrightarrow{D}^\mu H \right)^2$$

custodial breaking

$$\frac{c_y y_f}{f^2} |H|^2 \bar{f}_L H f_R + \text{h.c.}$$

$$\frac{c_6 \lambda}{f^2} |H|^6$$

■ **Form factor operators** (sensitive to the scale  $m_\rho$ )

$$\frac{ic_W}{2m_\rho^2} \left( H^\dagger \sigma^i \overleftrightarrow{D}^\mu H \right) (D^\nu W_{\mu\nu})^i$$

$$\frac{ic_B}{2m_\rho^2} \left( H^\dagger \overleftrightarrow{D}^\mu H \right) (\partial^\nu B_{\mu\nu})$$

$$\frac{ic_{HW}}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} (D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i$$

$$\frac{ic_{HB}}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}$$

minimal coupling:  $h \rightarrow \gamma Z$

loop-suppressed strong dynamics

$$\frac{c_\gamma}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} \frac{g^2}{g_\rho^2} H^\dagger H B_{\mu\nu} B^{\mu\nu}$$

$$\frac{c_g}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} \frac{y_t^2}{g_\rho^2} H^\dagger H G_{\mu\nu}^a G^{a\mu\nu}$$

Goldstone sym.

# Deformation of the SM Higgs: current constraints

$$\mathcal{L}_{\text{EWSB}} = \frac{v^2}{4} \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma) \left( 1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} \right) - \lambda \bar{\psi}_L \Sigma \psi_R \left( 1 + c \frac{h}{v} \right)$$

$\Sigma = e^{i\sigma^a \pi^a / v}$       Goldstone of  $SU(2)_L \times SU(2)_R / SU(2)_V$        $D_\mu \Sigma \approx W_\mu$

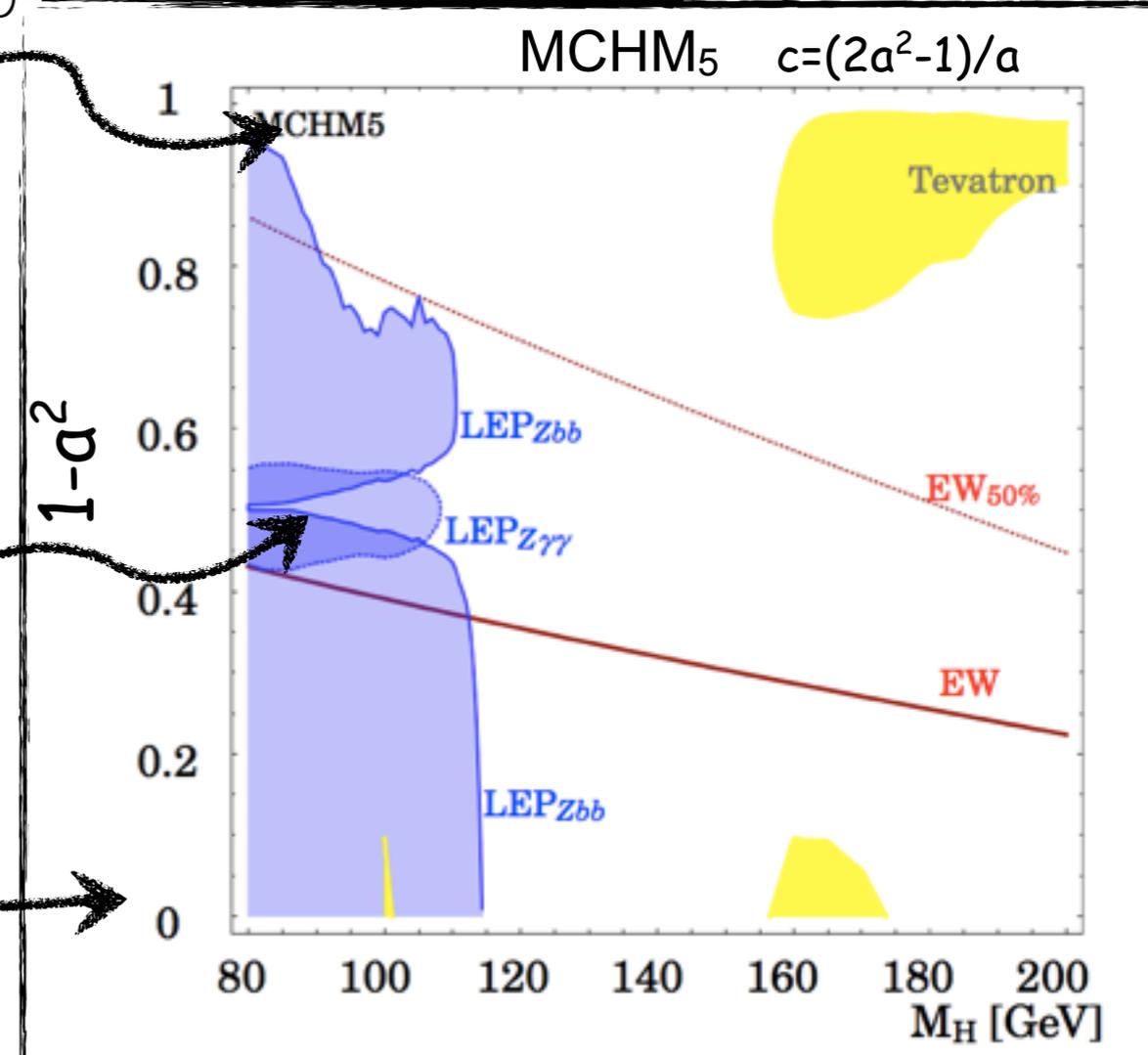
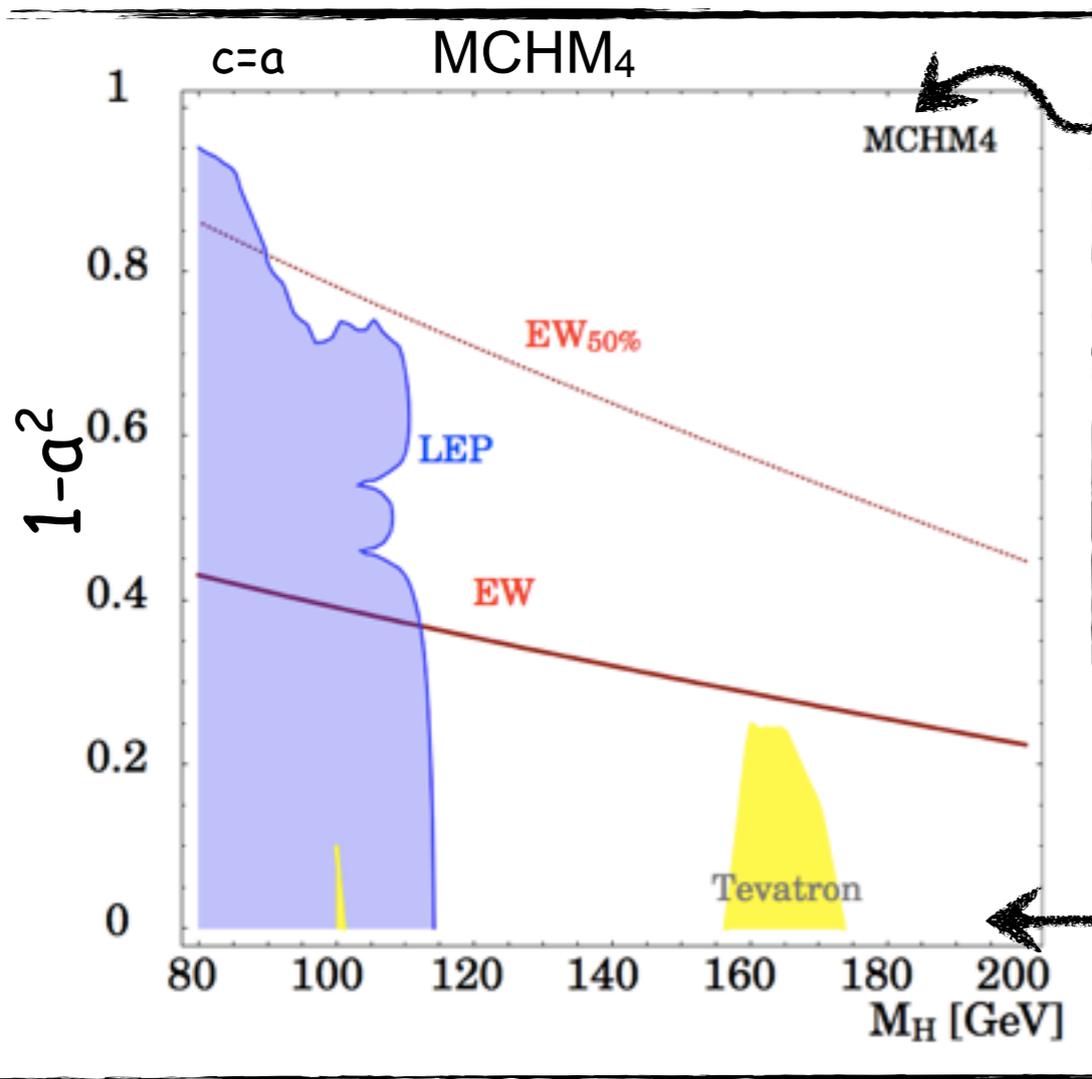
} SM 'a=1', 'b=1' & 'c=1' }  
 Current EW data constrain only 'a' (and marginally 'c')

Espinosa, Grojean, Muehlleitner '10

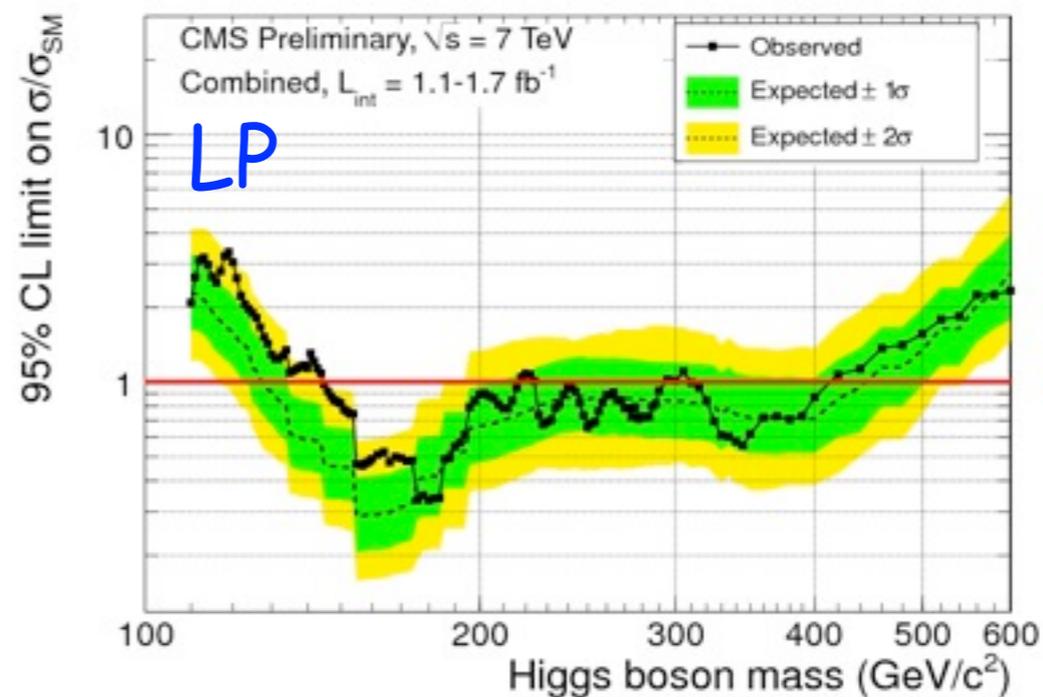
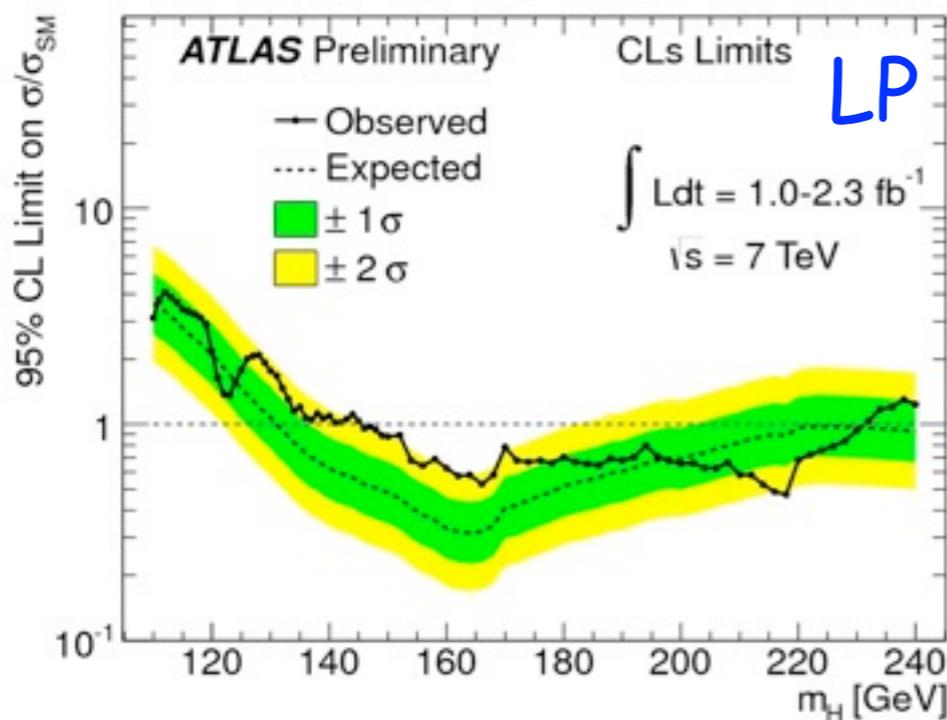
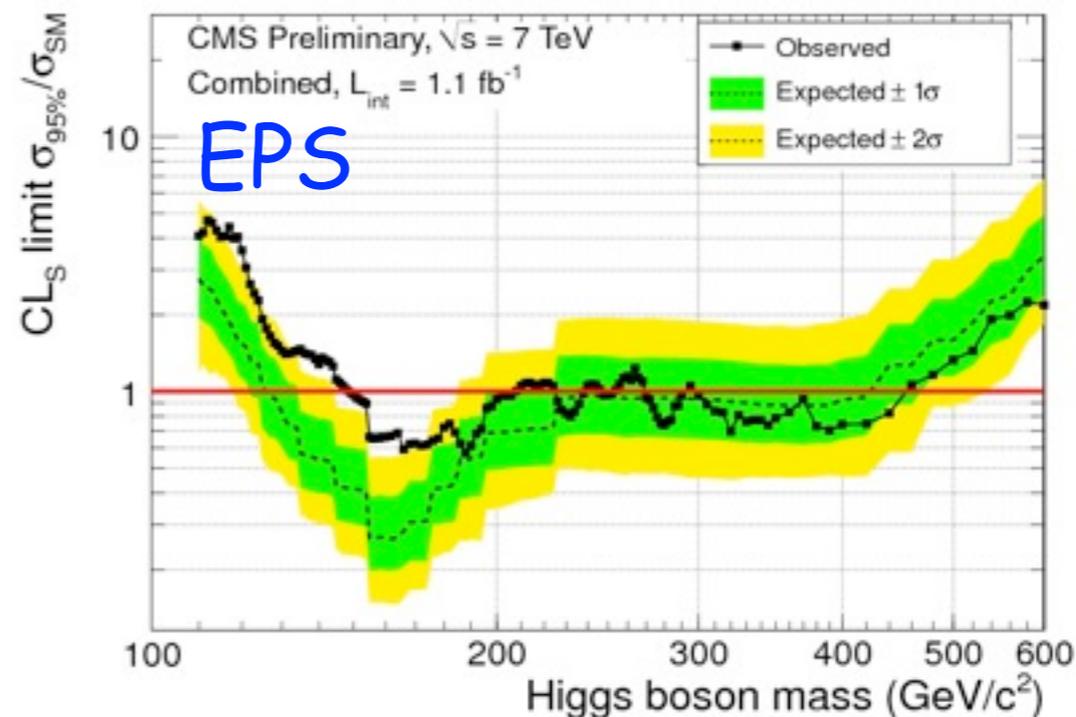
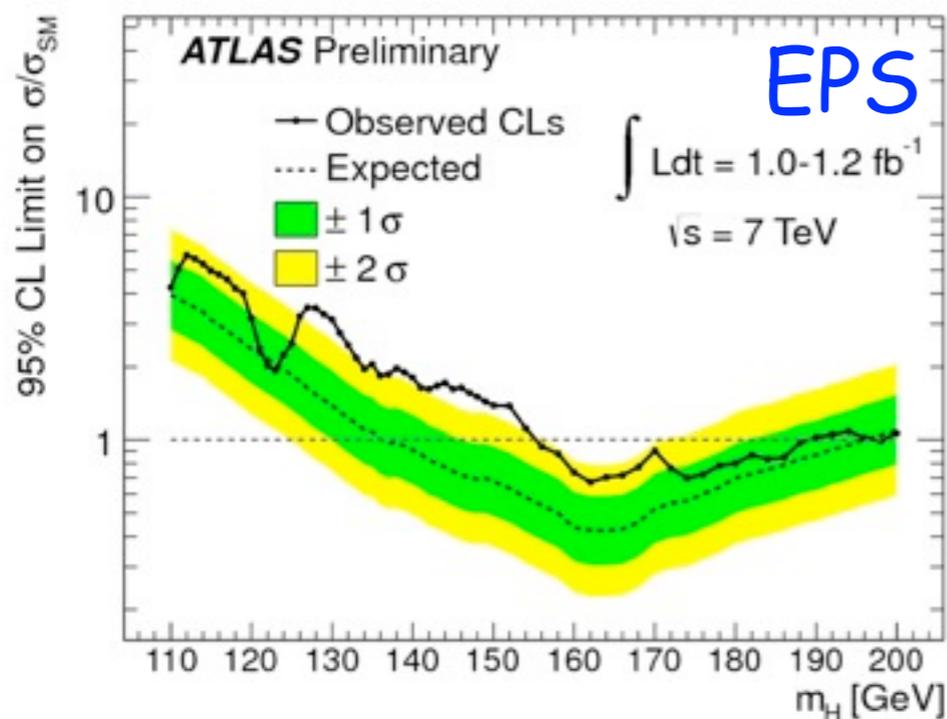
*gaugephobic Higgs*

*fermiophobic Higgs*

SM limits

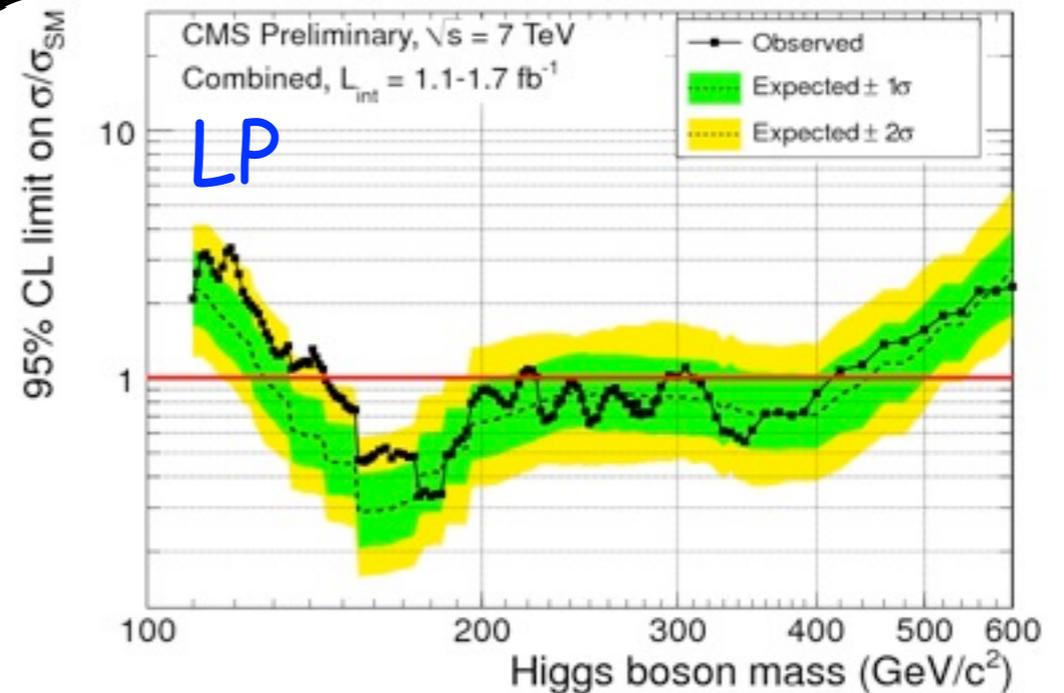
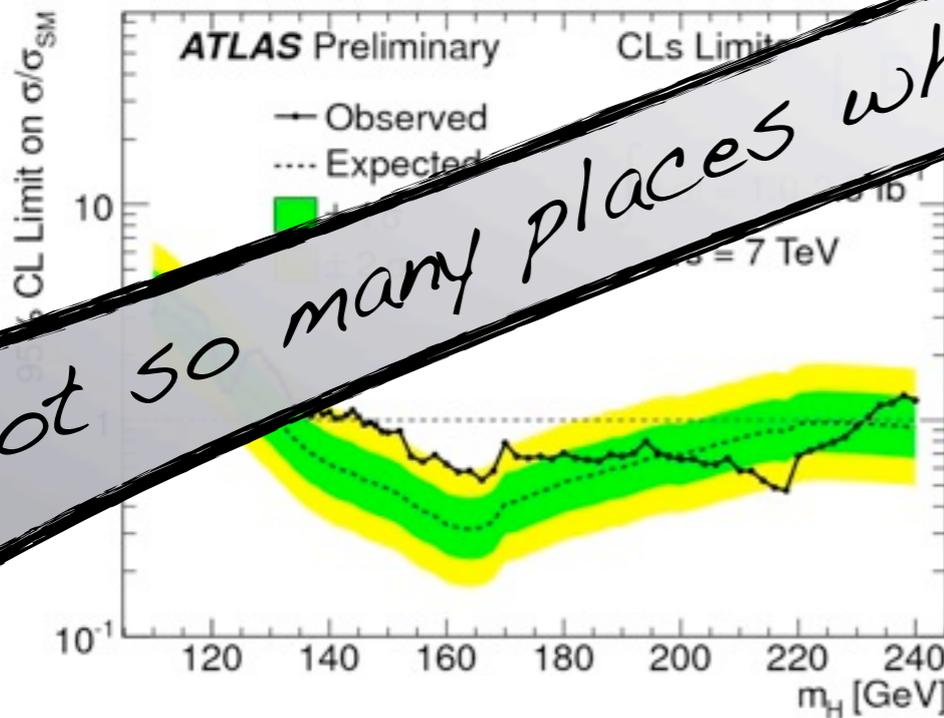
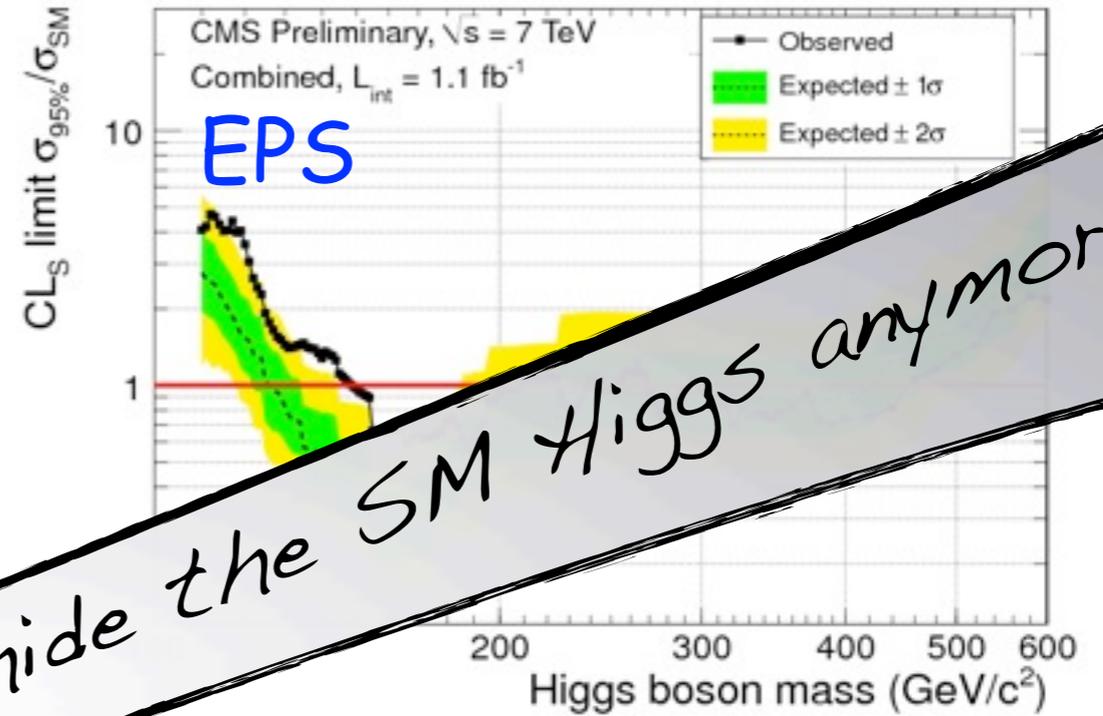
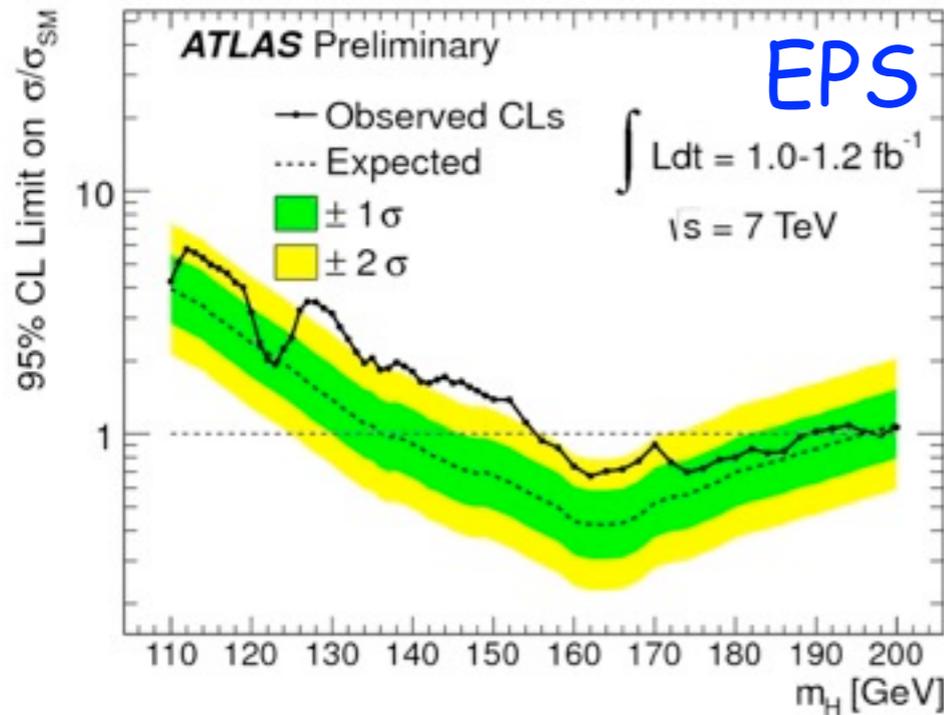


# Deformation of the SM Higgs: LHC constraints



LHC is now a Higgs exploring machine  
 (and it has quickly surpassed Tevatron)

# Deformation of the SM Higgs: LHC constraints



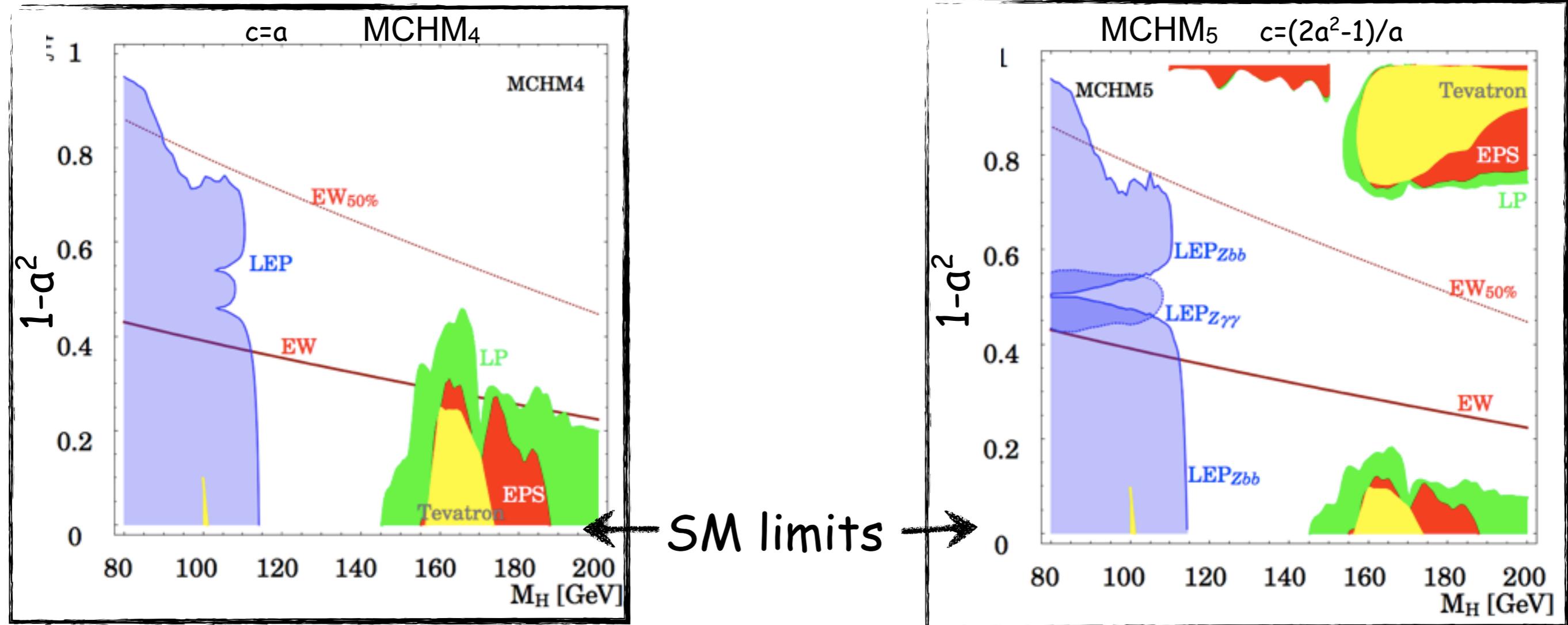
*not so many places where to hide the SM Higgs anymore*

LHC is now a Higgs exploring machine  
 (and it has quickly surpassed Tevatron)

# Deformation of the SM Higgs: LHC constraints

the SM exclusion bounds are easily rescaled in the  $(m_H, a)$  plane

Espinosa, Grojean, Muehlleitner '11

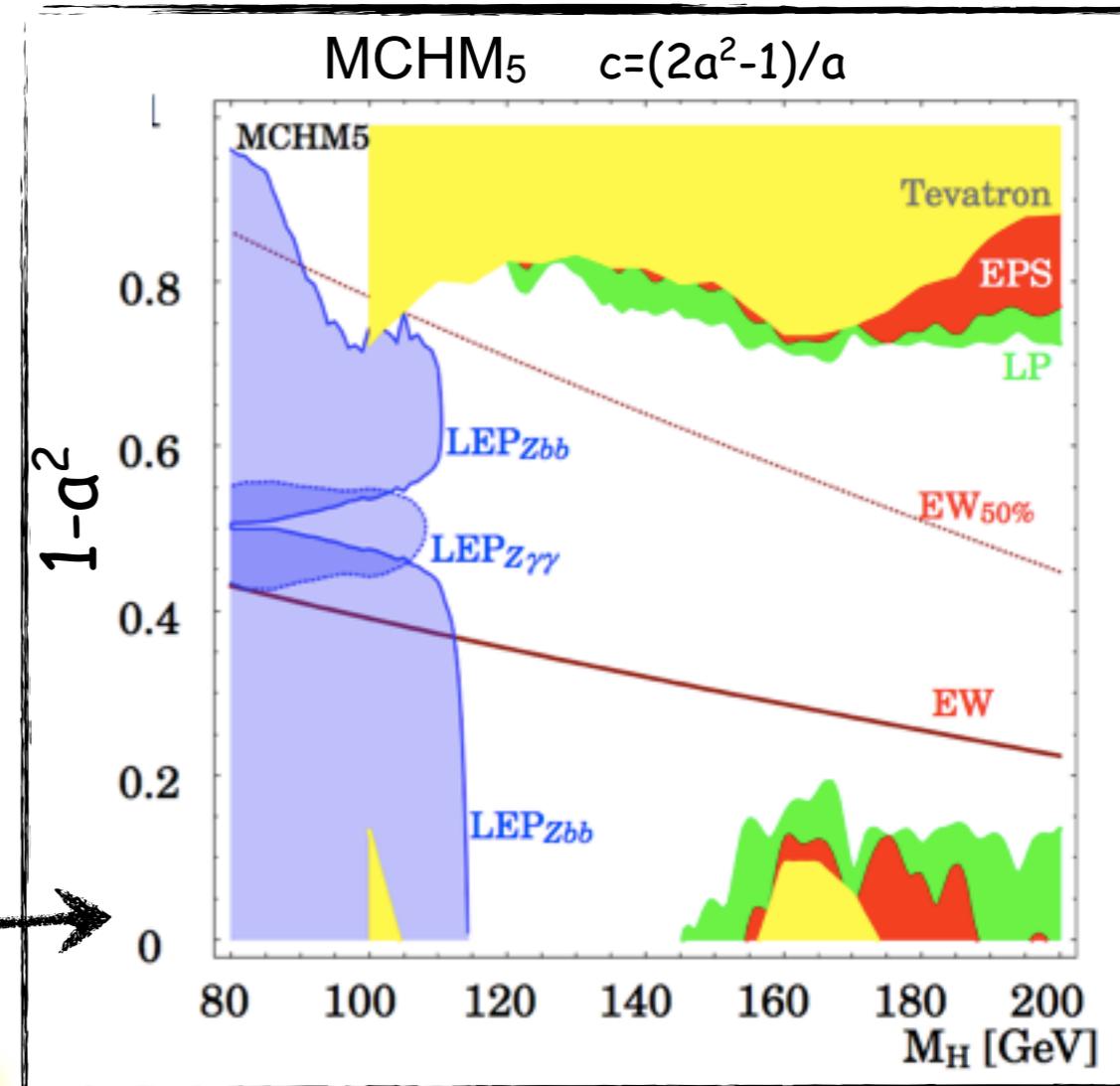
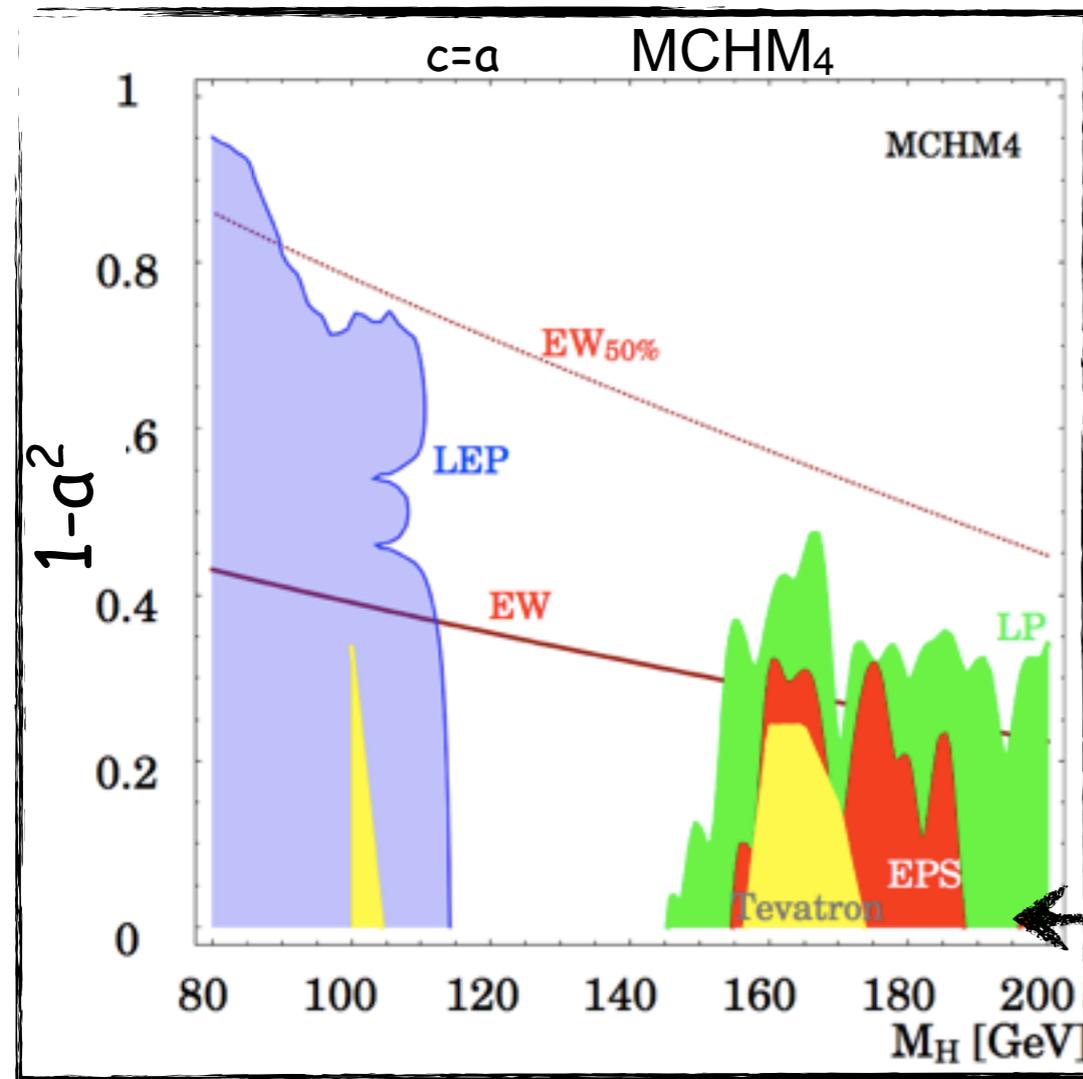


LHC is now a Higgs exploring machine  
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# Deformation of the SM Higgs: LHC constraints

the SM exclusion bounds are easily rescaled in the  $(m_H, a)$  plane

Espinosa, Grojean, Muehlleitner '11



SM limits

Be careful

- rescaling combination  $\neq$  combination of the rescaled channels  
(can be particularly important far away from SM)
- efficiency of the cuts may also depends on  $\xi$

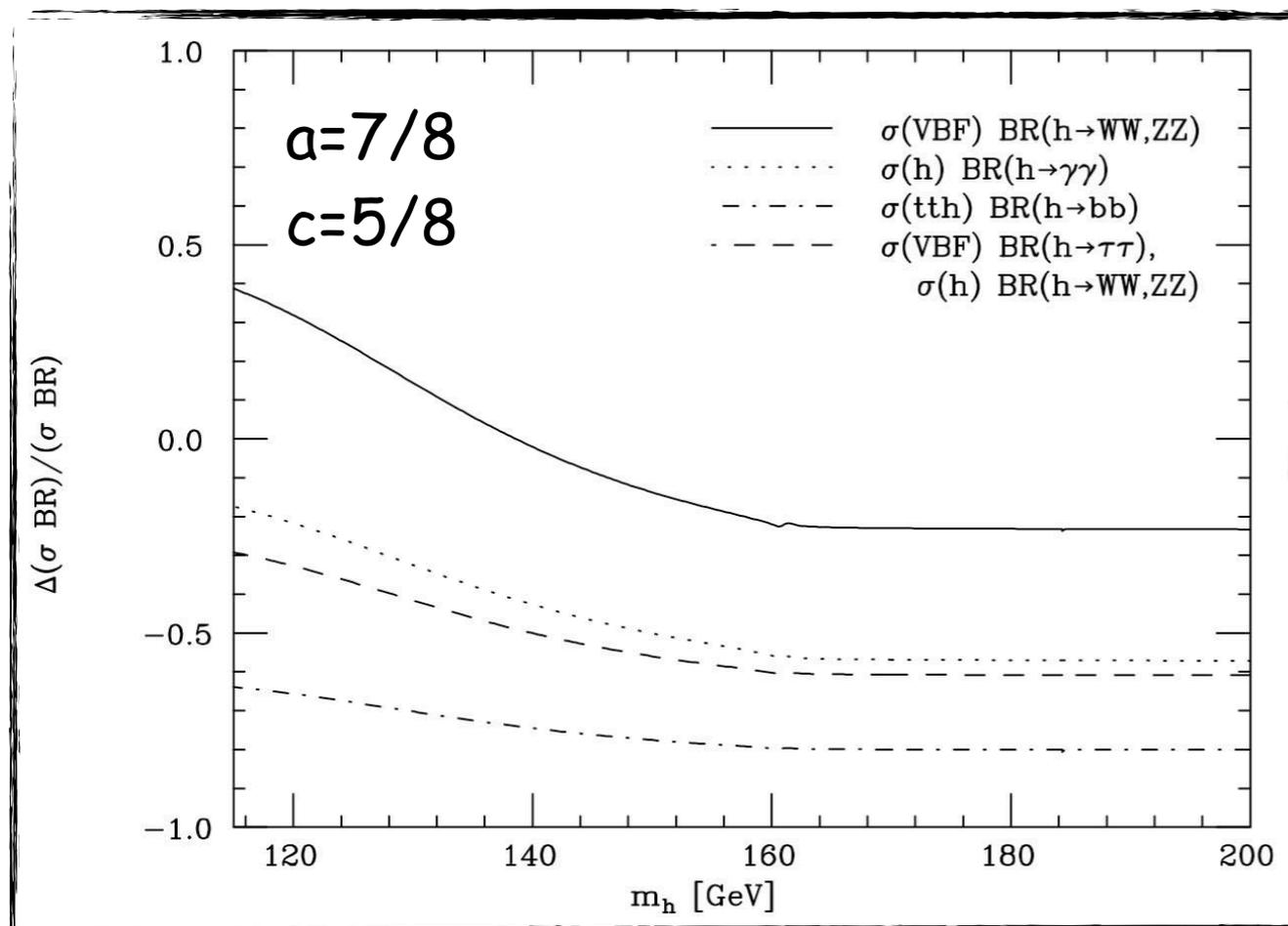
# Higgs anomalous couplings @ LHC

$$\mathcal{L}_{\text{EWSB}} = \frac{v^2}{4} \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma) \left( 1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} + b_3 \frac{h^3}{v^3} + \dots \right) - \lambda \bar{\psi}_L \Sigma \psi_R \left( 1 + c \frac{h}{v} + c_2 \frac{h^2}{v^2} + \dots \right)$$

$$a = \sqrt{1 - \xi} \quad b = 1 - 2\xi \quad b_3 = -\frac{4}{3}\xi \sqrt{1 - \xi} \quad c = \left( \sqrt{1 - \xi}, \frac{1 - 2\xi}{\sqrt{1 - \xi}} \right) \quad c_2 = -(\xi, 4\xi)$$

Minimal composite Higgs model (MCHM):  $SO(5)/SO(4)$

$$\Gamma(h \rightarrow f\bar{f}) = (2c - 1) \Gamma(h \rightarrow f\bar{f})_{\text{SM}} \quad \Gamma(h \rightarrow ZZ) = (2a - 1) \Gamma(h \rightarrow ZZ)_{\text{SM}}$$



Giudice, Grojean, Pomarol, Rattazzi '07

LHC can probe

$\Delta a$  &  $\Delta c$   
up to  $\sim 0.1 \div 0.2$   
i.e.  $4\pi f \sim 5 \div 7 \text{ TeV}$

compositeness scale of the Higgs  
(ILC/CLIC could go to few %, ie, test  
composite Higgs up to  $4\pi f \sim 30/60 \text{ TeV}$ )

How to probe the composite nature of the Higgs?

2. Strong scattering

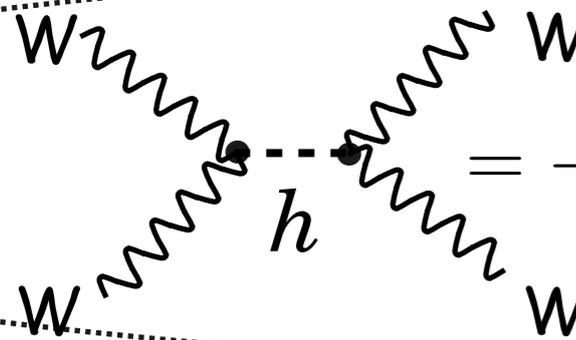


# How to probe the strong dynamics?

Look at pair production of strong states

Giudice, Grojean, Pomarol, Rattazzi '07

## strong WW scattering:



$$= -(1 - \xi)g^2 \frac{E^2}{M_W^2}$$

no exact cancellation  
of the growing amplitudes

$$\mathcal{A}(W_L^a W_L^b \rightarrow W_L^c W_L^d) = \mathcal{A}(s, t, u)\delta^{ab}\delta^{cd} + \mathcal{A}(t, s, u)\delta^{ac}\delta^{bd} + \mathcal{A}(u, t, s)\delta^{ad}\delta^{bc} \quad \mathcal{A} = \underbrace{(1 - a^2)}_{\frac{s}{f^2}} \frac{s}{v^2}$$

large  $\mathcal{L}_{int}$  needed

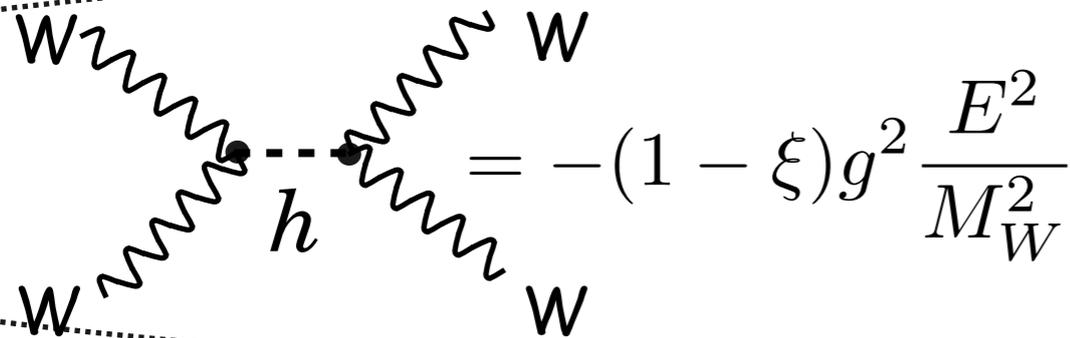
not competitive with the measurement of 'a' via anomalous couplings

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## strong double Higgs production:

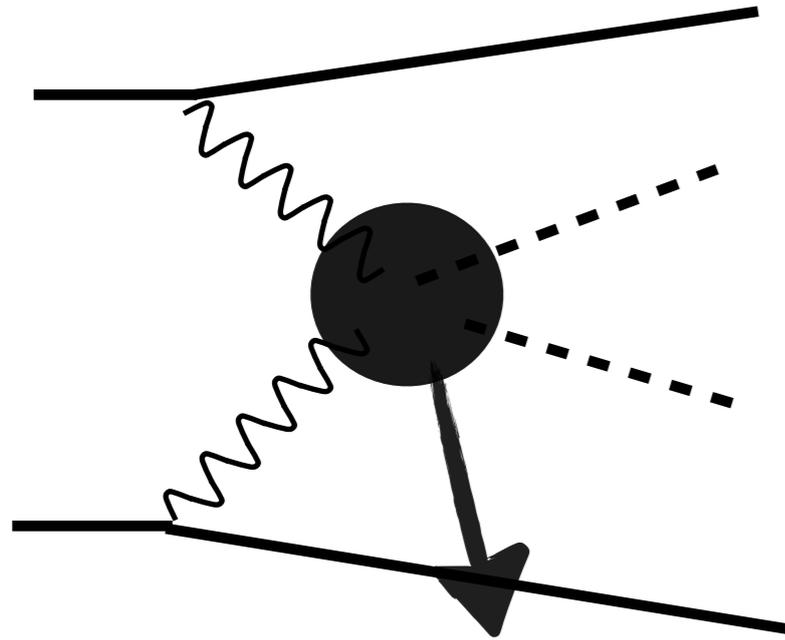
Contino, Grojean, Moretti, Piccinini, Rattazzi '10

$$\mathcal{A}(Z_L^0 Z_L^0 \rightarrow hh) = (W_L^+ W_L^- \rightarrow hh) = (b - a^2) \frac{s}{v^2}$$

access to a new interaction, 'b'

distinction between 'active' (higgs) and 'passive' (dilaton) scalar in EWSB dynamics

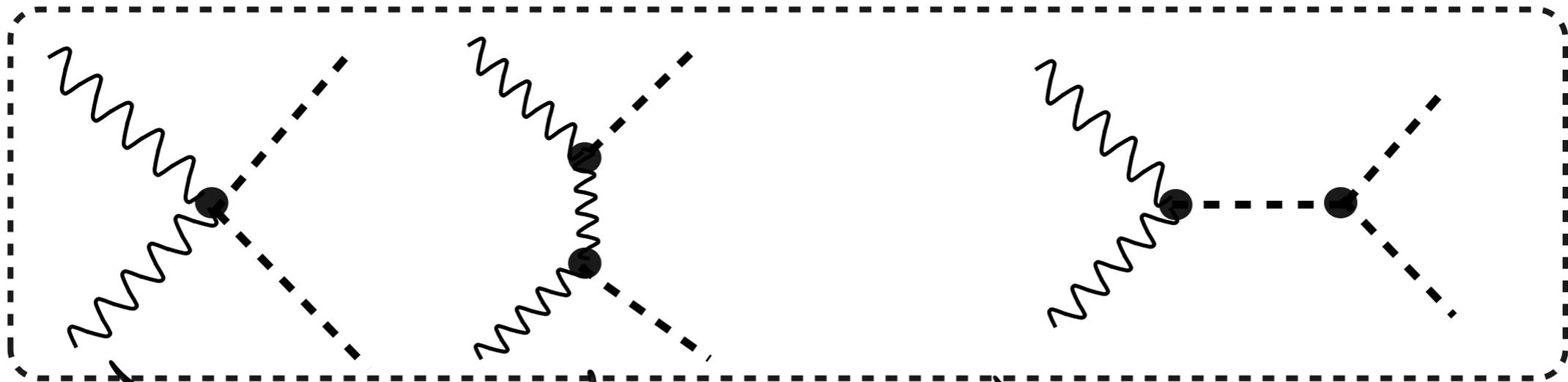
# Double Higgs production: 'b' and 'd<sub>3</sub>' couplings



$$\mathcal{L}_{\text{EWSB}} = \frac{v^2}{4} \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma) \left( 1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} \right)$$

$$V(h) = \frac{1}{2} m_h^2 h^2 + d_3 \frac{1}{6} \left( \frac{3m_h^2}{v} \right) h^3 + d_4 \frac{1}{24} \left( \frac{3m_h^2}{v^2} \right) h^4 + \dots$$

SM:  $a=b=d_3=d_4=1$



$$A \sim (b - a^2) \frac{4m_{hh}^2}{v^2}$$

$m_{hh}^2 \gg m_W^2$

asymptotic behavior  
sensitive to strong interaction

$$A \sim \text{cst.} + 3ad_3 \frac{m_h^2}{v^2}$$

$m_{hh}^2 \sim 4m_h^2$

threshold effect  
'anomalous coupling'

# Strong Higgs production: (3L+jets) analysis

Contino, Grojean, Moretti, Piccinini, Rattazzi '10

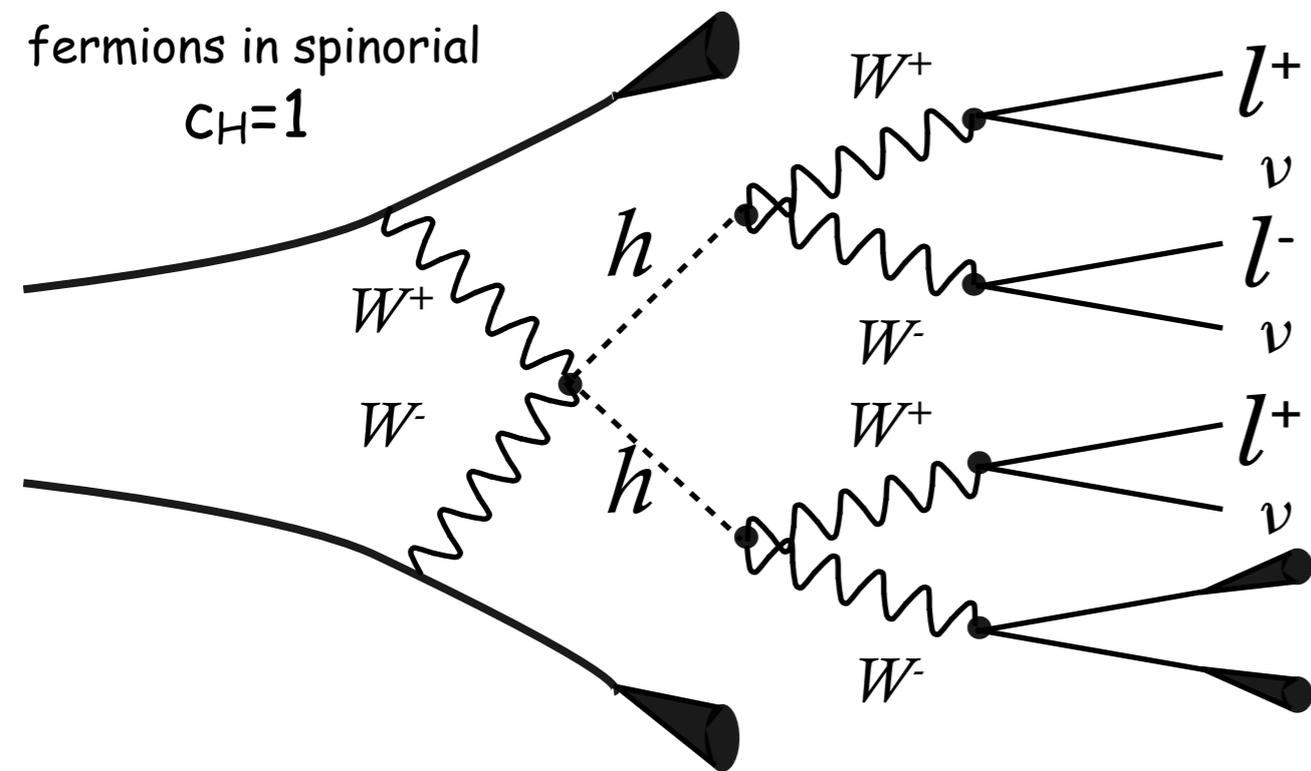
strong boson scattering  $\Leftrightarrow$  strong Higgs production

$$\mathcal{A}(Z_L^0 Z_L^0 \rightarrow hh) = \mathcal{A}(W_L^+ W_L^- \rightarrow hh) = \frac{c_H s}{f^2}$$

$m_h = 180$  GeV

fermions in spinorial

$c_H=1$



acceptance cuts	
jets	leptons
$p_T \geq 30$ GeV	$p_T \geq 20$ GeV
$\delta R_{jj} > 0.7$	$\delta R_{lj(ll)} > 0.4(0.2)$
$ \eta_j  \leq 5$	$ \eta_j  \leq 2.4$

Dominant backgrounds:  $Wll4j$ ,  $t\bar{t}W2j$ ,  $t\bar{t}2W(j)$ ,  $3W4j$ ...

forward jet-tag, back-to-back lepton, central jet-veto

$v/f$	1	$\sqrt{0.8}$	$\sqrt{0.5}$
significance @ $300 \text{ fb}^{-1}$	4.0	2.9	1.3
luminosity for $5\sigma$ ( $\text{fb}^{-1}$ )	450	850	3500

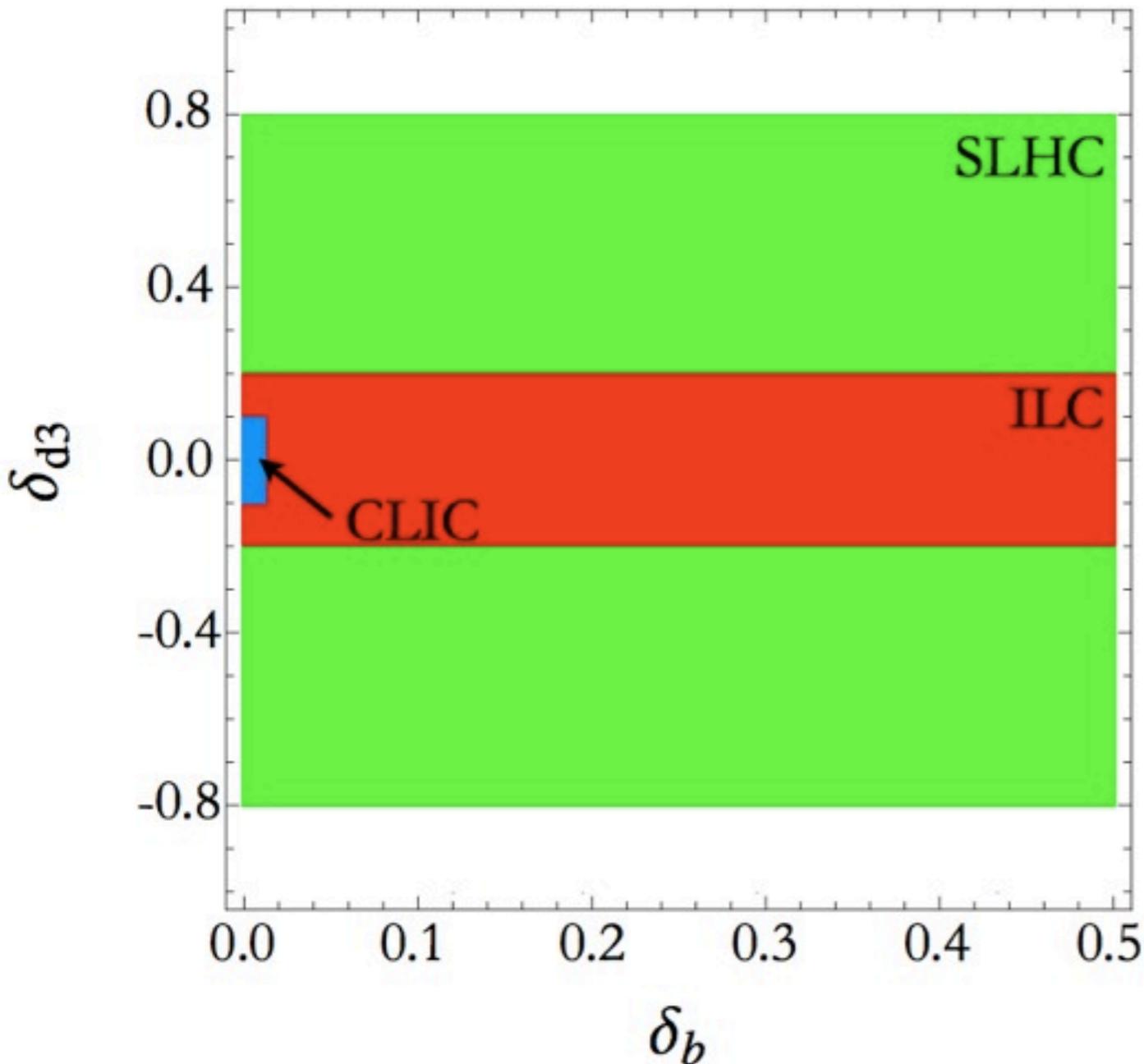
$\Leftarrow$  good motivation to SLHC

# Measuring the non-linearities of the Higgs

Contino, Grojean, Pappadopulo, Rattazzi, Thamm 'in progress

$$\mathcal{L}_{\text{EWSB}} = \frac{v^2}{4} \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma) \left( 1 + 2a \frac{h}{v} + b \frac{h^2}{v^2} \right)$$

$$V(h) = \frac{1}{2} m_h^2 h^2 + d_3 \frac{1}{6} \left( \frac{3m_h^2}{v} \right) h^3$$



- (S)LHC is barely sensitive to  $d_3$  and  $b$
- ILC has a sensitivity on  $d_3$  but not on  $b$
- CLIC can probe both  $d_3$  and  $b$

*How to probe the composite nature of the Higgs?*

*3. Identifying discrete symmetries of strong sector*



# Geometry of Coset from $W^+W^- \rightarrow 3h$

Contino, Grojean, Pappadopulo, Rattazzi, Thamm 'in progress

Strong

EWSB

$$\sigma_{2\pi \rightarrow 3\pi} \sim \frac{1}{8\pi} \frac{E^2}{f^4} \frac{E^2}{(4\pi f)^2}$$

$$E/f \leftrightarrow g$$

SM

$$\sigma_{2\pi \rightarrow 3\pi} \sim \frac{1}{8\pi} \frac{g^2}{v^2} \frac{g^2}{16\pi^2}$$

Probe of possible discrete symmetries in the strong dynamics

$G/H$  symmetric space

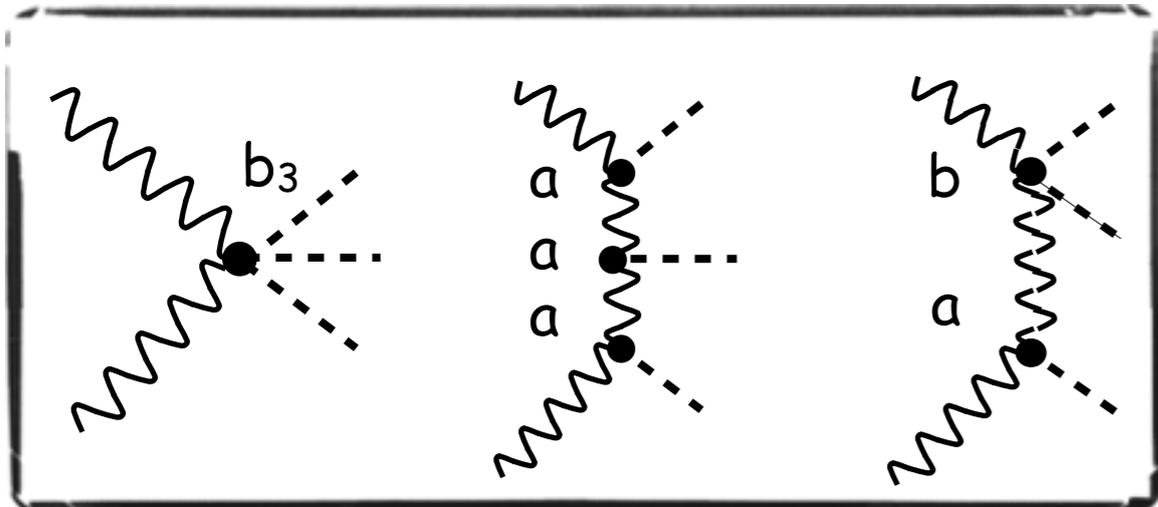


invariance under

$$\pi \rightarrow -\pi$$

a process with an odd # of PGBs

requires a coupling breaking the coset structure  
ie cannot be mediated by strong interactions alone



$$A_{WW \rightarrow 3h} \sim 4i \frac{s}{v^3} \left( \underbrace{a(b - a^2) - \frac{3}{4}b_3}_{=0 \text{ for symmetric coset}} \right) + \# s \times \underbrace{\left( \frac{m_W}{\sqrt{s}} \right)^2}_{\text{mediated by SM gauge interactions (breaking of coset structure)}}$$

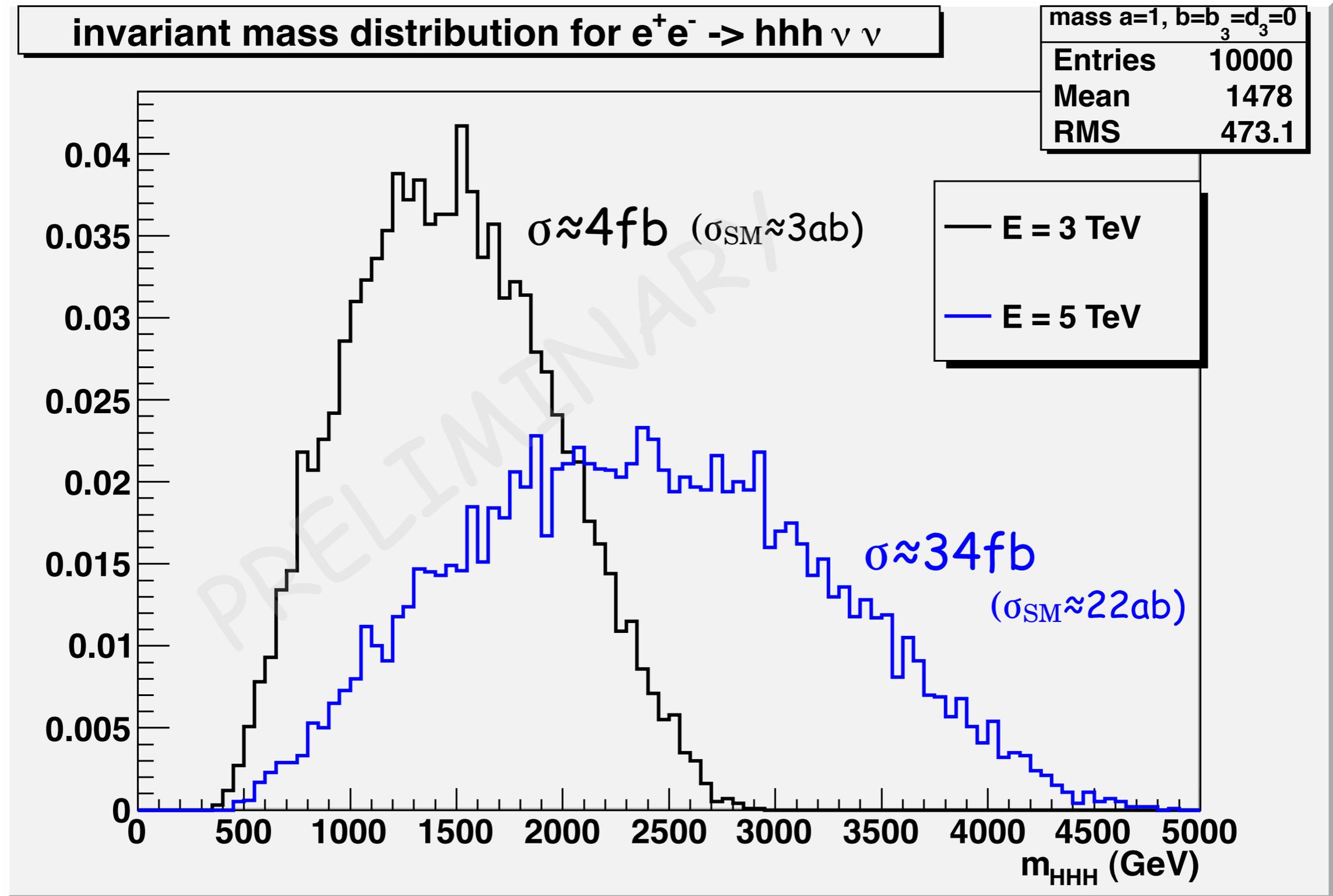
=0 for symmetric coset

mediated by SM gauge interactions (breaking of coset structure)

# $W^+W^- \rightarrow 3h @ CLIC$

Contino, Grojean, Pappadopoulo, Rattazzi, Thamm 'in progress

non-symmetric coset



*How to probe the composite nature of the Higgs?*

*4. Detecting heavy resonances*



# A heavy composite $W'$

Grojean, Salvioni, Torre '11

Observing a tower of resonances would be direct evidence of the strong interactions  
However, in the best configuration, LHC will have access to a few ones only

*How can we tell the difference between a massive gauge field  
and a resonance from a strong sector?*

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*elementary spin-1*

$$g=2 \Leftrightarrow \Lambda \gg M/e \Leftrightarrow W' \rightarrow W\gamma \text{ highly suppressed}$$

gyromagnetic ratio of any elementary particle of mass  $M$   
coupled to photon must be  $g=2$  at tree-level to maintain  
perturbative unitarity up to energy  $\Lambda \gg M/e$

Ferrara, Porrati, Telegdi '92

$$(g-1)B^{\mu\nu}W_{\mu}^{\prime+}W_{\nu}^{\prime-}$$

dimension-4 operator mediating  $W' \rightarrow W\gamma$  after  $W$ - $W'$  mixing

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Ferrara, Porrati, Telegdi '92

*composite spin-1*

$$g \neq 2 \ \& \ \Lambda > 5\div 10 M \Leftrightarrow W' \rightarrow W\gamma \text{ allowed and potentially large}$$

$$(g-1)B^{\mu\nu}W_{\mu}^{\prime+}W_{\nu}^{\prime-}$$

dimension-4 operator mediating  $W' \rightarrow W\gamma$  after  $W$ - $W'$  mixing

# Conclusions

EW interactions need Goldstone bosons to provide mass to  $W, Z$



EW interactions also need a UV moderator/new physics  
to unitarize  $WW$  scattering amplitude

We'll need another Gargamelle experiment  
to discover the still missing neutral current of the SM: the Higgs  
weak NC  $\Leftrightarrow$  gauge principle  
Higgs NC  $\Leftrightarrow$  ?

Strong EWSB w/o an elementary Higgs can be very similar to SM  
it might take some time to decipher the true dynamics of EWSB!

"Higgs = emergency tire of the SM"

Altarelli @ Blois'10

# An Emergency Tire Even Beyond the SM

"Higgs = emergency tire of the SM"

Altarelli @ Blois'10



[picture courtesy to Andreas Weiler]